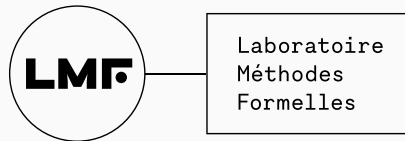


# Using Ghost Ownership to Verify Union-Find and Persistent Arrays in Rust

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PARIS-SACLAY

# Shared XOR mutable

Aliasing restrictions in Rust:

```
fn f(x: &mut i32, y: &mut i32) {  
    *x = 1; *y = 2;  
    assert!(*x == 1);  
}
```

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f(x, x); // X compile error
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But not for unsafe code/raw pointers!

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unsafe fn f(x: *mut i32, y: *mut i32) {  
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These makes verification easier

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Creusot  leverages this:

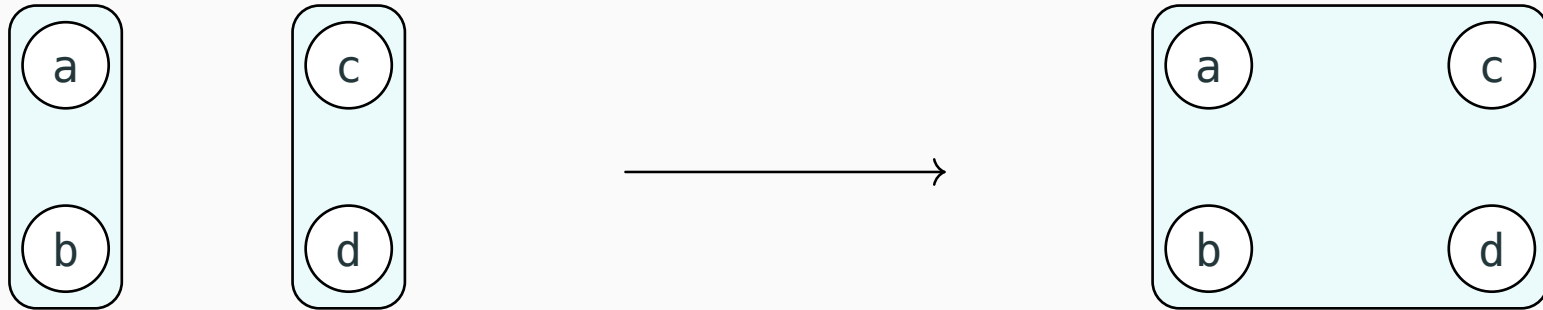
```
#[requires(true)]  
#[ensures(^x == 1 && ^y == 2)]  
fn f(x: &mut i32, y: &mut i32) {  
    *x = 1; *y = 2;  
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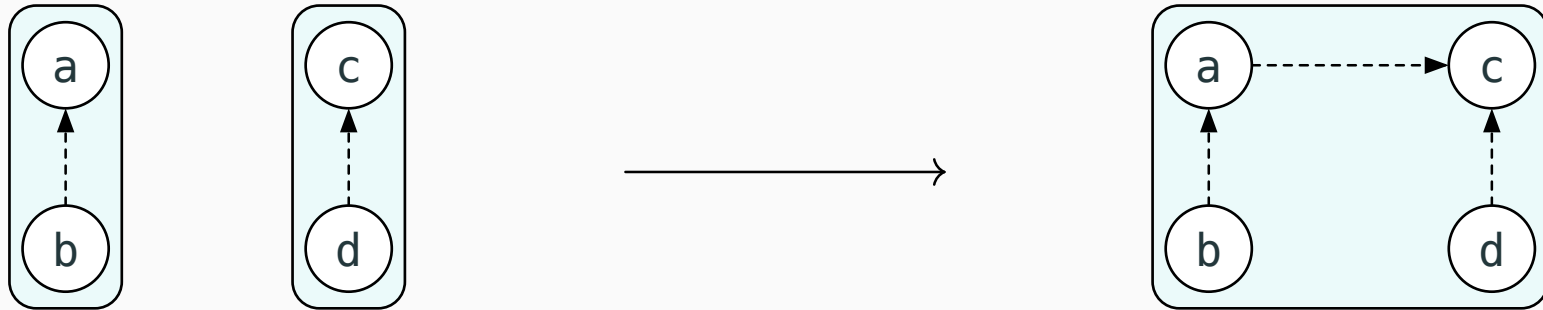
We still want to implement and verify pointer-based data structures.

Categorize elements into sets



```
union(b, d);
```

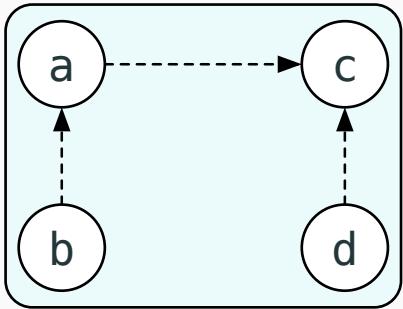
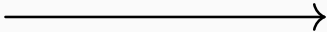
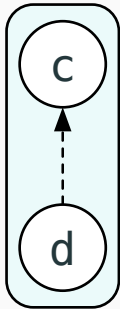
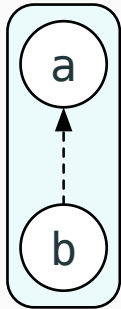
Categorize elements into sets



```
union(b, d);
```

# Union-find

Categorize elements into sets



```
find(a) != find(c);
```

```
union(b, d);
```

```
find(a) == find(c)
```

Alternative implementation: use an array, passed as parameter.

```
fn find(a: &mut Vec<Node>, elem: usize) -> usize;
```

# Union-find

Alternative implementation: use an array, passed as parameter.

Our solution:

- Pointers in the code;
- Global state in **ghost code**, passed as parameter.

→ Ownership of this state needs to be tracked in ghost code.

```
fn find(gh: Ghost<&mut ...>, elem: *mut Node) -> *mut Node;
```

Adapted ghost code with ownership (from Verus) in Creusot.

Support for most pointer operations → verify idiomatic Rust code.

Can verify union-find's implementation.

Cannot dereference raw pointers as-is.

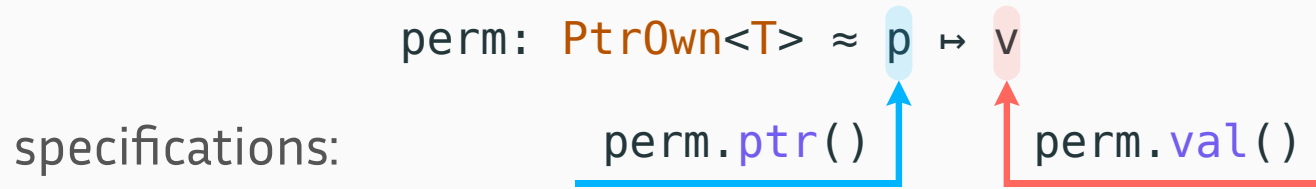
Instead, use `Ghost<PtrOwn<T>>`:

- Ghost-only
- Has ownership

Data stored in `Ghost<T>` is erased at runtime:

| for Creusot  | for rustc   |
|--|---|
| <pre data-bbox="129 539 1041 829">#[requires(**x == 1)] fn f(x: Ghost&lt;Box&lt;i32&gt;&gt;) {     let y1 = x;     let y2 = x; // x compile error }</pre>                            | <pre data-bbox="1144 602 1534 829">fn f(x: ()) {     let y1 = x;     let y2 = x; }</pre>              |
| <ul data-bbox="129 882 728 1001" style="list-style-type: none"> <li>• <code>Ghost&lt;T&gt;</code> <math>\approx</math> <code>T</code> logically</li> <li>• borrow checked</li> </ul> | <ul data-bbox="1144 882 1680 938" style="list-style-type: none"> <li>• no memory footprint</li> </ul> |

perm: PtrOwn<T>  $\approx$  p  $\mapsto$  v



perm: `PtrOwn<T>`  $\approx$  `p`  $\mapsto$  `v`  
 specifications: `perm.ptr()` `perm.val()`

code:

|        |  |
|--------|--|
| Create | <code>let (p, perm): (*mut T, Ghost&lt;PtrOwn&lt;T&gt;&gt;) = PtrOwn::new(v);</code> |
| Read   | <code>let x: &amp;T = PtrOwn::as_ref(p, perm.borrow());</code>                       |
| Write  | <code>let x: &amp;mut T = PtrOwn::as_mut(p, perm.borrow_mut());</code>               |

# Specification for `as_mut`

```
#[requires(ptr == perm.ptr())]
#[ensures(^perm.ptr() == perm.ptr())]
#[ensures(*result == perm.val())]
#[ensures(^perm.val() == ^result)]
pub unsafe fn as_mut(ptr: *mut T, perm: Ghost<&mut PtrOwn<T>>) -> &mut T;
```

```
// perm ≈ p ↦ v
let bor = PtrOwn::as_mut(ptr, perm.borrow_mut());
*bor = *bor + 1;
// perm ≈ p' ↦ v'
```

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// perm ≈ p ↦ v
let bor = PtrOwn::as_mut(ptr, perm.borrow_mut());
*bor = *bor + 1;
// perm ≈ p ↦ v + 1
```

# Union-find

```
enum Node { Root, Link(*mut Node) }

struct UF { // wrapped in Ghost
  perms: FMap<*mut Node, PtrOwn<Node>>,
  // ...
}

impl Invariant for UF {
  #[logic]
  fn invariant(self) -> bool {
    forall<p: *mut Node> self.perms.contains(p) ==>
      self.perms[p].ptr() == p &&
      match self.perms[p].val() {
        // ...
      }
  }
}
```

# Proof of find

```
fn find(                                ptr: *mut Node) -> *mut Node {  
    match unsafe { &*ptr } {  
        // ...  
    }  
}
```

# Proof of find

```
struct UF {  
    perms: FMap<*mut Node, PtrOwn<Node>>  
}
```

```
#[requires(uf.contains(ptr))]  
#[ensures(result == uf.root_of(ptr))]  
fn find(mut uf: Ghost<&mut UF>, ptr: *mut Node) -> *mut Node {  
    let perm: Ghost<&PtrOwn<Node>> = ?;  
    match *PtrOwn::as_ref(ptr, perm) {  
        // ...  
    }  
}
```

# Proof of find

```
struct UF {  
    perms: FMap<*mut Node, PtrOwn<Node>>  
}
```

```
#[requires(uf.contains(ptr))]  
#[ensures(result == uf.root_of(ptr))]  
fn find(mut uf: Ghost<&mut UF>, ptr: *mut Node) -> *mut Node {  
    let perm: Ghost<&PtrOwn<Node>> = ghost!(&uf.perms[ptr]);  
    match *PtrOwn::as_ref(ptr, perm) {  
        // ...  
    }  
}
```

# Ghost code

```
let x: Box<i32>          = Box::new(1);
let gh: Ghost<Box<i32>> = ghost!(Box::new(1));
let inner = *gh;        X
ghost! {
    let x_ref = &x;      ✓
    let x_mutref = &mut x; X
    let x_owned = x;     X

    let inner = *gh;     ✓
    let gh_owned = gh;   ✓
    let gh_ref = &gh;    ✓
    let gh_mutref = &mut gh; ✓

    return; break; continue; X
};
```

# Conclusion

- In this talk:
  - Ghost code with ownership with `Ghost` and `ghost!`.
  - Support for pointers via `PtrOwn`.
  - Proof of union-find's implementation.
- In the paper:
  - Resource algebras and local invariants.
  - Proof of persistent arrays' implementation.

Proofs are in Creusot's repository: <https://github.com/creusot-rs/creusot>

